

# Higher Geometry & Measures Answers

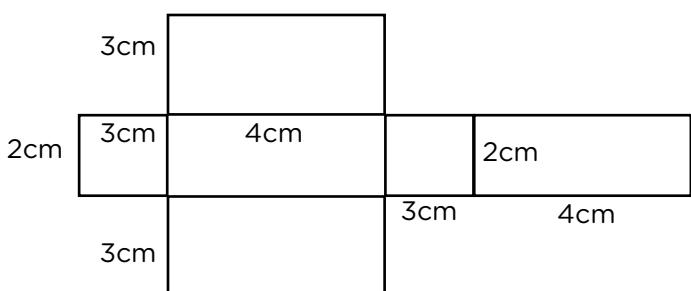
## GCSE Mathematics



### Starters

Parallel Lines	Opposite angles are equal and internal angles add to $180^\circ$	(1)
	$81 + a + 67 = 180$	(1)
	$a = 32^\circ$	(1)

Perpendicular Bisector	Arc from each point drawn	(1)
	Line joining intersections	(1)

Nets	 A net for a rectangular prism. It consists of a top rectangle (3cm by 4cm), four side faces (2cm high), and two front/back faces (3cm by 4cm). The side faces are positioned between the top and bottom rectangles.	(1)
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Trigonometric Values	$\sin 30^\circ = \frac{1}{2}$	(1)
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Angles in a Circle	$x = 102^\circ$ cyclic quadrilateral adds to $180^\circ$	(1)
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Pythagoras' Theorem	$4.9^2 + 6.2^2 = AC^2$
	$AC = 7.9\text{cm}$

### Main Course

I am sailing	$\tan O = 5.2/3.6 \quad O = 55.3$	(1)
	$\text{Bearing A from B } 90^\circ - 55.3 = 034.7^\circ$	(1)
	$\cos 55.3 = 3.6/h$	(1)
	$h = 6.32\text{km}$	(1)

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Angles in a Pentagon	$\text{Max } x = 540 - (93.5 + 86.5 + 107.5 + 118.5)$ (1) $= 134^\circ$ (1)
	$\text{Min } x = 540 - (94.5 + 87.5 + 108.5 + 119.5)$ (1) $= 130^\circ$ (1)
Vectors	$\overrightarrow{AB} = -3\mathbf{a} + 2\mathbf{b}$ (1) $\overrightarrow{OP} = 3\mathbf{a} + \frac{3}{4}(-3\mathbf{a} + 2\mathbf{b})$ (1) $= \frac{3}{4}\mathbf{a} + \frac{3}{2}\mathbf{b}$ (1)
Baseball	$\text{Angle BPF} = 180 - (36+46) = 98^\circ$ (1) $\frac{\text{BF}}{\sin 98} = \frac{18.39}{\sin 36}$ (1) $\text{BF} = 30.98\text{m}$ (1)
Filling the Sink	$\text{Volume} = \frac{4}{3}\pi 30^3 \times \frac{1}{2} / 1000$ (1) $= 18\pi \text{ litres}$ (1) $= 240 \div 60 = 4 \text{ litres a minute}$ (1) $= 18\pi \div 4 = 14 \text{ minutes}$ (1)
Anyone for Tea?	$\text{Volume of kettle} = \frac{12393\pi}{5}$ (1) $\text{Volume of Mug} = 300\pi$ (1) $\text{No of mugs filled} = 8 \text{ full cups}$ (1) $\text{Remaining water } 0.25 \text{ litres}$ (1)

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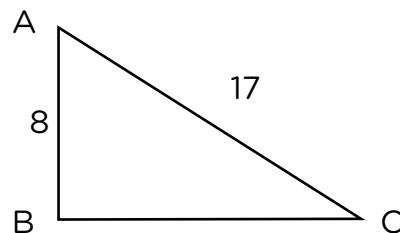


### Dessert

Trigonometry

$$BC = \sqrt{17^2 - 8^2} = 15 \quad (1)$$

$$\cos \theta = \frac{15}{17} \quad (1)$$



Angles in Polygons

Internal angle for equilateral triangle =  $60^\circ$

Internal angle for square =  $90^\circ$

Internal angle for regular hexagon =  $120^\circ$  (1)

For shapes to tessellate internal angles must add to  $360^\circ$

$$120 + 90 + 90 + 60 = 360^\circ \quad (1)$$

Surface Area of Cylinder

$$SA = 2\pi r^2 + 2\pi rh \quad (1)$$

$$= 2\pi r(r + h) \quad (1)$$

Circle Theorems

Angle CBE =  $70^\circ$  = Angle BDE opposite interior angle (1)

Angle ODB =  $55^\circ$  triangle is isosceles so angle BOD =  $70^\circ$  (1)

Angle BED =  $35^\circ$  angle at circumference half angle at centre (1)

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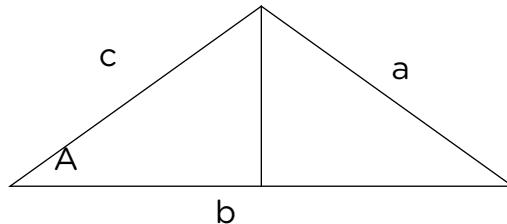


### Area of Triangle

$$\sin A = \frac{\text{height}}{c} \quad \text{so } h = c \times \sin A \quad (1)$$

$$\text{Area} = \frac{1}{2} \times \text{base} \times \text{height} \quad (1)$$

$$= \frac{1}{2} \times b \times c \times \sin A \quad (1)$$



### Volume Ratios

If heights same height of cone =  $2r$  (1)

$$\text{Vol Cone} = \frac{2}{3} \pi r^3 \quad (1)$$

$$\frac{2}{3} \pi r^3 : \frac{4}{3} \pi r^3 \quad (1)$$

$$1 : 2 \quad (1)$$

### Drinks

$$360 - 242 = 118^\circ \quad (1)$$

$$180 - 118 = 062^\circ \quad (1)$$

### Loci

Two points 5cm apart (1)

Circle 1 - radius 3cm and Circle 2  
radius 3.5cm (1)

Shade region that intersects (1)

### Angle of a Sector

$$\frac{\theta}{360} \times \pi \times 4.5^2 = 24 \quad (1)$$

$$\theta = \frac{24}{\pi \times 4.5^2} \times 360 \quad (1)$$

$$= 135.8^\circ \quad (1)$$

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## Area of Similar Shapes

$$56 \times 50^2 = 140\ 000 \text{ cm}^2 \quad (1)$$

$$= 14m^2$$

## Angles in Triangles

$$\frac{\sin BAC}{5.9} = \frac{\sin 32}{7.2} \quad (1)$$

$$BAC = \sin^{-1} \frac{5.9 \times \sin 32}{7.2} \quad (1)$$

$$= 25.7^\circ \quad (1)$$

## Enlargement

Triangle (-1,1) (-5,1) (-5,-7) (2)